## 38 Distribution networks

- A corporate ladder network that combines 4 identical loads $Z_{L}$ into a single equivalent input impedance $Z_{L}$ is shown in the margin.
- In this network 6 different quarter-wave transformers with arbitrary but identical characteristic impedances $Z_{o}$ are utilized.

You should be able to compute the load voltages $V_{L}$ in the network in terms of input voltage $V_{\text {in }}$ applied across the input port by using the current-forcing formula for the quarter-wave transformer introduced earlier on.


By symmetry, the loads absorb equal avg power, a quarter of the input power each.

- If, in a corporate ladder network, $Z_{L}=Z_{o}$, then TL segment lengths connected to each $Z_{L}$ can be varied at will without affecting the input impedance $Z_{L}=Z_{o}$ (why?).
- Allowing variable length TL's connected to each $Z_{L}$ makes it possible to adjust and vary the phase of the voltage and current of each $Z_{L}$ - this is useful, for instance, in feeding phased antenna arrays $\left(Z_{L}\right.$ represents an antenna load) to achieve steerable radiation patterns.
- A hybrid combiner network shown in the margin can be used to excite two identical TL loads $R$ (e.g., antenna arrays impedance matched to have input impedances $R$ ) with independent signal generators $V_{A}$ and $V_{B}$ having equal internal resistances $R$ matched to the load resistance.
- The hybrid "rat-race" combiner is built with 6 quarter-wave transformers of identical

$$
Z_{o}=\sqrt{2} R,
$$

HYBRID COMBINER --- SUM and DIFFERENCE OF ISOLATED GENERATOR SIGNALS V_A AND V_B ARE APPLIED TO LOADS R

in which case the generators $V_{A}$ and $V_{B}$ see impedance-matched loads (at the hybrid inputs where they are connected) and produce load voltages proportional to $V_{A} \pm V_{B}$ as shown in the diagram.

- Generators A and B with open ckt voltages $V_{A}$ and $V_{B}$ are isolated from one another's influence because of "destructive interference" between the two paths from each generator to the other one (two paths have a $\frac{\lambda}{2}$ length difference).
- This very special situation allows one to calculate the various terminal voltages on the hybrid due to $V_{A}$ and $V_{B}$ one-at-a-time as if loads $R$ were isolated from generator-B and -A (by "virtual shorts" existing across generator terminals when $V_{B}$ and $V_{A}$ are suppressed) in turns, and then superpose the results.
- Terminal voltages obtained with that procedure (those shown on the diagram) turn out to be valid when both generators are active as can easily be checked for selfconsistency by using the current-forcing equations introduced earlier. For instance, the total current into generator-A terminal (flowing from both sides) is

$$
I_{A}=-\frac{j}{R \sqrt{2}}\left(-j \frac{V_{A}-V_{B}}{2 \sqrt{2}}\right)-\frac{j}{R \sqrt{2}}\left(-j \frac{V_{A}+V_{B}}{2 \sqrt{2}}\right)=-\frac{V_{A}}{2 R},
$$

and hence the voltage drop from the same terminal to the ground is

$$
I_{A} R+V_{A}=-\frac{V_{A}}{2 R} R+V_{A}=\frac{V_{A}}{2}
$$

as marked explicitly on the diagram. All self-consistency tests that can be applied with the given expressions are passed, and so the results given are valid.

- The input and output ports of a hybrid combiner can be swapped while still maintaining the properties of the hybrid - namely, input impedance $R$, and output signals the sum and difference of generator voltages.


